

**Comments on "IV quantile regression for group-level treatments,
with an application to the distributional effects of trade"
by Denis Chetverikov, Brad Larsen, and Christopher Palmer**

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Introduction

- This paper discusses econometric methods that relate to a substantial section of applied work, so it is a good choice for an Interactions workshop.
- It provides a practical framework for estimating distributional effects, asymptotic properties for their method, and evidence of computational and empirical applicability.
- A tour de force around a simple theme, all accomplished with great skill.
- I will provide a summary of the paper and some general remarks.

Summary

- Concerned with applications where the interest is in the effect of a group-level policy on the group-level distribution of some individual characteristic.
- An example of their approach is a linear regression of a quantile q_g^τ on a variable x_g :

$$q_g^\tau = \gamma(\tau) + \beta(\tau) x_g + \varepsilon_g(\tau) \quad g = 1, \dots, G \quad \tau \in (0, 1)$$

where $\varepsilon_g(\tau)$ is an error term orthogonal to x_g .

- In their setting x_g is observed but q_g^τ is not. So it is replaced by a sample quantile \hat{q}_g^τ obtained from individual-level data (of size N_g).
- Since \hat{q}_g^τ is not an unbiased estimate of q_g^τ , consistency for $\beta(\tau)$ of a regression of \hat{q}_g^τ on x_g requires large G and large N_1, \dots, N_G .
- In an IV version of the problem $\varepsilon_g(\tau)$ is correlated with x_g but not with an instrument w_g that satisfies the rank and exclusion conditions.
- In a more general version \hat{q}_g^τ , instead of a sample quantile, is a sample QR coefficient (intercept or slope) involving individual-level covariates.
- The paper provides an asymptotic normality result for $\sqrt{G} \left(\hat{\beta}(\cdot) - \beta(\cdot) \right)$ as long as N_g grows sufficiently fast as $G \rightarrow \infty$ (a mild requirement).
- It also provides an estimator of the asymptotic covariance function.
- These are all useful results.

1. Group-level causality and individual-level causality

- A natural context for the current framework is group-level causality.
- A formulation for a population of groups is as follows. A potential outcome is a random function (a cdf) rather than a r.v. and treatment takes place at group-level.
- Larsen (2014) and Autor, Dorn, and Hanson (2013)'s extension are nice examples.
- In Larsen a group is a state-year cell, treatment is a teacher certification law, and a potential outcome is the cdf of teacher quality in a state-year under some licensing law
- Group-level issues are eg the exogeneity of licensing laws across states & years, or possible spillover effects. But the group-level perspective is silent about what goes on at the individual level.
- One could think of each group as a separate market for teacher quality, the equilibrium outcome of which is a cdf of teacher quality that is affected by licensing laws through supply and demand channels.

Individual-level causality

- The same model can also be regarded as a model for an individual potential outcome:

$$y_{ig} = \gamma(u_{ig}) + \beta(u_{ig}) x_g + \varepsilon(u_{ig}, \eta_g)$$

where $u_{ig} \sim \mathcal{U}(0, 1)$ indep. of (x_g, η_g) and $\varepsilon_g(\tau) = \varepsilon(\tau, \eta_g)$ for arbitrary $\dim(\eta_g)$.

- y_{ig} is the individual outcome whose group quantile function is q_g^τ (teacher's i quality).
- There is a single individual unobservable u_{ig} and many group unobservables η_g .
- x_g is always exogenous w.r.t. to u_{ig} but may or may not be exogenous w.r.t. η_g .
- As a model of individual potential outcomes, $\beta(u_{ig}) \Delta x$ would measure the causal effect of a change Δx on individual's i outcome.
- The model assumes comonotonicity (rank invariance) at individual and group levels.
- This is an unappealing model of individual response in applications such as those in Larsen or ADH where occupational entry/exit is a relevant aspect of the response.

Point-wise comparison of quantiles

- A point-wise comparison of quantiles gives the shape of individual treatment gains under comonotonicity, but it is not an obvious metric in a group-level comparison of distributions from different populations.
- The function $\widehat{\beta}(\tau)$ is not necessarily an interpretable distributional treatment effect at group level, so is not to be taken for granted as the focus of empirical reporting.
- It may be more natural to look at changes in distributional measures motivated in substantive considerations, such as inequality indices, polarization, or probabilities of exceeding a preestablished threshold.
- A situation where the interest is in comparing distributions of outcomes of different populations, rather than in the distribution of individual changes in a fixed population.

2. Reducing the dimensionality of group effects

- There is a trade-off between allowing for large or low dimensional unobservable group-effects and the scope of nonparametric identification.
- Application of the present method is straightforward as it proceeds in a quantile-by-quantile fashion allowing for a different error at each quantile.
- However, if the number of individual observations per group is small the incidental parameter problem is a challenge.
- Moreover, while being agnostic about the group-factor dimension is attractive, often substantive knowledge suggests that only a small no. of underlying factors play a role.
- Whether one uses a model with a different group effect at each quantile or one with a small number of group effects may have implications for fixed- N_g identification.
- For example, Rosen (2010) shows that a fixed-effects panel model for a single quantile is not point identified.

Group-level analysis when the number of observations per group is small

- Arellano & Bonhomme (2013) show that a QR model with a scalar group effect is nonparametrically identified in panel data with $N_g = 3$ under completeness conditions.
- They consider the fixed- N_g identification and estimation of functions Q_{yi} and Q_α :

$$\begin{aligned}y_{ig} &= Q_{yi}(z_{ig}, \alpha_g, u_{ig}) \\ \alpha_g &= Q_\alpha(z_g, v_g)\end{aligned}$$

where α_g is a group-effect, $z_g = \{z_{ig}\}_{i=1}^{N_g}$, and $u_{ig} \mid (z_g, \alpha_g)$ and $v_g \mid z_g$ are $\mathcal{U}(0, 1)$.

- A centered measure of location on the pdf of $y_{ig} \mid z_{ig}, \alpha_g$ for some i is imposed.
- If z_{ig} includes an i -invariant x_g , the result may hold for a reparameterization that subsumes x_g .
- Exploring conditions (such as within variability in Q_{yi}) under which derivative effects of Q_{yi} w.r.t. x_g can be disentangled is an interesting question.

Group-level analysis when N_g is small (continued)

- If the interest is in individual-level effects, Q_{y_i} is the main response function and Q_α is a nuisance function.
- If the interest is in group-level effects, Q_{y_i} is an aggregator that produces the factors α_g and Q_α is a group-level response function.
- In the IV situation, a similar reinterpretation of the micro setup conditionally on (x_g, w_g) leads to identification of the joint density of (α_g, x_g, w_g) .
- The question here is how to control the small- N_g noise in a nonparametric way so that one can still say something about the effect of x_g on the group-level cdf of y_{ig} .

3. Standard errors

- Chamberlain (1994) considered a version of the estimator in this paper motivated in the distributional analysis of censored earnings data.
- He analyzed the properties of $\widehat{\beta}(\tau)$ when G is fixed, N_g is large, and there are no group-level unobservables (except for model misspecification).
- Chamberlain's standard errors are the mirror image of those considered here.
- In his case all sampling error comes from the discrepancy between \widehat{q}_g^τ and q_g^τ whereas this is ignored in the asymptotics here leading to standard errors driven by $\varepsilon_g(\tau)$.
- Chamberlain's situation is similar to DiD case-studies where G and/or the number of treated groups are small.
- A reinterpretation of $\widehat{\beta}(\tau)$ in those cases is as an estimate of the infeasible fixed- G sample statistic that uses group-level population quantiles.
- Desirable to report standard errors that are robust to alternative asymptotic plans.
- For example, standard errors for fixed- N_g pseudo-true values that retain double asymptotic validity.
- Ignoring the first stage may come at a cost in finite samples.

4. Hausman-Taylor internal instruments

- The setting for the Hausman-Taylor estimator is a model of the form

$$y_{ig} = \gamma z_{ig} + \beta x_g + \eta_g + v_{ig}$$

where z_{ig} is uncorrelated with η_g but x_g is not, and both are v_{ig} -exogenous.

- The idea is to use z_{ig} as an instrument for itself and \bar{z}_g as an instrument for x_g .
- The method works as long as \bar{z}_g is correlated with the observed component of the group-effect (x_g) but not with the unobserved one (η_g).
- In panel data there are not many applications of this idea due to difficulty in finding time-varying covariates that can be thought a priori as being fixed-effect exogenous.
- A related common practice is to look at predictive effects on group-level unobservables, be intercepts or slopes.
- This paper emphasizes the benefits from being able to use internal instruments, but I was under the impression that they did not feature prominently in their examples.
- Perhaps they have in mind exploiting the micro-data to construct aggregate instruments more generally, but it would be nice to see more examples where internal instruments determine the empirical force of the results.

Concluding remarks

- In group-level comparisons of potential cdf-outcomes is not obvious that we want to focus on point-wise comparisons of quantiles, which are reminiscent of comonotonic individual-level effects.
- There is a trade-off between double asymptotic approaches with high dimensional group-level unobservables and approaches with fewer group-level unobservables that deliver nonparametric identification when the number of units per group is small.
- Standard errors that exhibit robustness to alternative asymptotic plans are attractive in applications that combine group-level data and micro data.